Delhi School of Economics Department of Economics

Entrance Examination for M.A. Economics Option A Series 01

June 30, 2007

Time: 3 hours

Maximum marks: 100

General Instructions: Please read carefully.

- Do not break the seal on this booklet until instructed to do so by the invigilator. Anyone breaking the seal prematurely will be evicted from the examination hall and his/her candidature will be cancelled.
- Immediately on receipt of this booklet, fill in your Name and Roll Number in the designated space below.
- Check that you have a bubble-sheet accompanying this examination booklet.
- · Following the instructions on the bubble-sheet, fill in the required information in Boxes 1, 2, 4, 5 and 6 on the bubble-sheet. The invigilator will sign in Box 3. In Box 4, enter your Roll Number as a 4-digit number with preceding zeros, e.g. 0012 or 0123. In Box 6, enter 01 as your series number.
- Keep your admission ticket easily accessible for verification by the invigilators.
- The entire examination will be checked by a machine. Therefore, it is very important that you follow the instructions on the bubble-sheet.
- · For rough work (calculations, drawing etc.), use only the blank pages at the end of this booklet. The rough work will not be read or checked.
- When you finish, hand in this booklet and the bubble-sheet to the invigilator.
- Do not disturb or talk to your neighbours at any time. Anyone engaging in illegal examination practices will be immediately evicted and that person's candidature will be cancelled.
- Only after the invigilator announces the start of the examination, break the seal on this booklet and follow the instruction on Page 2.

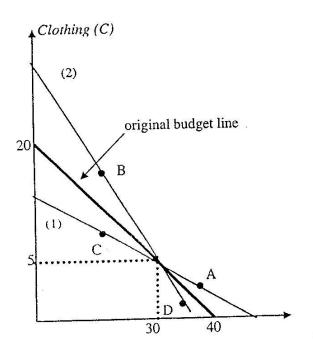
Full Name	
Roll Number	

PART I: One-mark questions

Instructions:

- First check that this booklet has pages numbered 1 through 24. Also check that the bottom of every page is marked AS01. Bring any missing pages to the attention of the in rigilator.
- This part of the examination consists of 20 multiple-choice questions. Each question is followed by four possible answers, one of which is correct. Indicate the correct answer on the bubble-sheet, NOT on this booklet.
- Each correct choice will earn you 1 mark. However, you will lose 1/3 mark for each incorrect choice. If you shade none of the bubbles or more than one bubble, you will get 0 for that question.
- · You may begin now. Good luck.
- 1. Consider a consumer having a utility function U=2x+y where x and y are two commodities. Suppose that the price of x and y are both Rs. 5 each and the consumer's income is Rs. 100. In equilibrium, the consumer will consume the bundle
 - (a)(10,10)
 - (b)(0,20)
 - (c)(20,0)
 - (d) none of the above
- 2. With quantity of x on the horizontal axis, the Engel curve for commodity x corresponding to the utility function U=y+f(x) will be
 - (a) a ray through the origin
 - (b) a vertical line
 - (c) a horizontal line
 - (d) a curve with an inflexion point
- 3. Suppose a producer has a fixed coefficient technology Q=Min(2K, 3L), where Q is output and K and L are the inputs. At equilibrium
 - (a) K=L
 - (b) K=(3/2)L
 - (c) K=(2/3)L
 - (d) K and L are indeterminate
- 4. A monopolist will never produce a quantity where the price elasticity of demand is inelastic because:
 - (a) P > MC in such a case
 - (b) MR > MC in such a case
 - (c) MR < 0 in such a case
 - (d) P < ATC in such a case

- 5. In the figure below when the budget line (drawn in bold) was originally 5F + 10 C = 200, Anita purchased 30 units of F and 5 units of C. At two later dates, lines (1) and (2) were the budget lines. Anita had the same preferences in all three instances. As a rational consumer, which market baskets might she have purchased at the later dates?
 - (a) A, B
 - (b) A, D
 - (c) B, C
 - (d) C, D



Food(F)

- 6. NAIRU implies
 - (a) the unemployment rate is zero
 - (b) inflation is constant
 - (c) the rate of growth of real GDP is constant
 - (d) none of the above
- In an open economy with perfect capital mobility and fixed exchange rates, an open market operation will
 - (a) increase output and reduce interest rate
 - (b) increase the money supply
 - (c) lower the trade deficit
 - (d) change the composition of the monetary base
- 8. If a person is a borrower, a rise in the interest rate will
 - (a) always reduce borrowing

- (b) always increase borrowing
- (c) could increase borrowing depending on the relative strengths of income and substitution effects.
- (d) none of the above.
- 9. The J-curve suggests that the effect of an appreciation of the exchange rate on the trade balance is to:
 - (a) improve it in the short run
 - (b) worsen it in the short run
 - (c) leave it unchanged
 - (d) improve it in the long run.
- 10. Under classical supply conditions, a fiscal expansion
 - (a) only raises the price level and the interest rate
 - (b) expands supply at constant prices
 - (c) expands supply at rising prices
 - (d) leaves both supply and price level unchanged
- 11. Consider the following functions $f: \mathbb{R} \to \mathbb{R}$, where \mathbb{R} denotes the set of real numbers. Which of the following functions is quasi-convex?
 - (a) $f(x) = x^2$
 - (b) $f(x) = \cos x$
 - $(c) f(x) = e^{-x}$
 - (d) $f(x) = x^{-1}$ if $x \neq 0$; f(x) = 0 if x = 0
- 12. Consider an $n \times n$ matrix A with real entries. If matrix B is derived by adding the first column of A to the last column of A, then
 - (a) $\det A < \det B$
 - (b) $\det A > \det B$
 - (c) $\det A = \det B$
 - (d) the sign of $\det A$ is the opposite of the sign of $\det B$
- 13. Consider a strictly decreasing (i.e., x > y implies f(x) < f(y)) and differentiable function $f: \Re \to \Re$, where \Re denotes the set of real numbers. Denote the derivative of f at $x \in \Re$ by Df(x). Which of the following may be true about f?
 - (a) Df(x) > 0 for some $x \in \Re$
 - (b) Df(x) = 0 for some $x \in \Re$
 - (c) Df(x) = 0 for every $x \in (a, b)$ where a < b
 - (d) $Df(x) \ge 0$ for every $x \in \Re$
- 14. If the statement "There exists a legislature and a party such that every legislator in that party pays taxes" is false, then which of the following statements must be true?
 - (a) In every legislature and every party, all legislators do not pay taxes.
 - (b) There exists a legislature such that every legislator in every party does not pay taxes.
 - (c) In every legislature, there exists a party and a legislator in that party who does

not pay taxes.

- (d) In every legislature and every party, there exists a legislator who does not pay taxes.
- 15. If $f: \mathbb{R}^n \to \mathbb{R}$ is twice differentiable, concave and homogeneous of degree 1, then the Hessian matrix of f is
 - (a) negative definite
 - (b) positive definite
 - (c) singular
 - (d) non-singular
- 16. Consider an experiment in which five fibers having different lengths are subjecting to a testing process to learn which fiber will break first. The lengths of the five fibers are 1 inch, 2 inches, 3 inches, 4 inches and 5 inches. Suppose the probability that any fiber will be the first to break is proportional to the length of that fiber. The probability that the length of the fiber that breaks first is not more than 3 inches is:
 - (a) 3/5
 - (b) 2/5
 - (c) 1/3
 - (d) 2/3
- 17. Which of the following statements is WRONG: A probability density function f(x)
 - (a) can be used to model a continuous variable
 - (b) integrates to 1 over the range of x
 - (c) increases steadily from 0 to 1
 - (d) must be greater than or equal to 0 over the range of x
- 18. A primary school has 6 classes, numbered from 1 to 6. Class 1 has twice as many students as each of the other classes. What is the probability that a randomly selected student is from an odd-numbered class?
 - (a) 10/21
 - (b) 3/7
 - (c) 8/21
 - (d) 4/7
- 19. A traffic light on the way to the University is red 40% of the time. What's the probability of getting a red light (i) 2 days in a row; (ii) any 2 out of 3 days.
 - (a) (i) 0.16; (ii) 0.20
 - (b) (i) 0.16; (ii) 0.29
 - (c) (i) 0.24; (ii) 0.29
 - (d) none of the above
- 20. Let Y denote the number of heads obtained when 3 coins are tossed. The variance of Y^2 is:
 - (a) 6.5
 - (b) 7.0
 - (c) 7.5
 - (d) 8.0

PART II: Two-mark questions

Instructions:

- This part of the examination consists of 40 multiple-choice questions. Each question
 is followed by four possible answers, one of which is correct. Indicate the correct
 answer on the bubble-sheet, NOT on this booklet.
- Each correct choice will earn you 2 marks. However, you will lose 2/3 mark for each incorrect choice. If you shade none of the bubbles or more than one bubble, you will get 0 for that question.
- 21. A firm has the production function $Q = 12L L^2$, where L is labour input and Q is output. If the firm is a monopolist with a demand curve P(Q) = 100 Q, what is the MRP_L (Marginal Revenue Product of Labour) curve?
 - (a) $1200 288L + 72L^2 4L^3$
 - (b) $1200 288L 72L^2 + 4L^3$
 - (c) $1200 488L + 72L^2 4L^3$
 - (d) $1200 488L 72L^2 + 4L^3$
- 22. Sudhir lives in Gujarat. His total wealth next year, including his house, will be Rs. 5,00,000. There is a 10 percent chance that a big earthquake will occur next year and completely destroy his house, valued at Rs. 2,00,000.
 - (i) What is Sudhir's expected wealth next year if he chooses not to buy house insurance?
 - (ii) Suppose Sudhir's utility function is given by $U(W) = W^{0.5}$, where W represents total wealth in thousands of rupees. Is Sudhir risk-averse, risk-loving, or risk-neutral?
 - (a) (i) Rs. 4,50,000 and (ii) risk-averse
 - (b) (i) Rs. 4,50,000 and (ii) risk-neutral
 - (c) (i) Rs. 4,80,000 and (ii) risk-loving
 - (d) (i) Rs. 4,80,000 and (ii) risk-averse
- 23. Consider an airport that produces noise (N) that declines as the distance (d) in kilometers, from the airport increases: $N(d) = 1/d^2$. Praful works at the airport. Praful's damage from noise is Rupee 1 per unit of noise and is associated with where Praful lives. His costs of commuting are Rupee 1 per kilometer (each way). The closest he can live to the airport is d = 0.1 km.
 - (i) What is the distance Praful will live from the airport in the absence of compensation for the noise?
 - (ii) Suppose Praful is compensated for his damage, wherever he may live. How much will he be compensated?

- (a) (i) 1 km and (ii) Rs. 100
- (b) (i) 0.1 km and (ii) Rs. 100
- (c) (i) 1 km and (ii) Rs. 1
- (d) (i) 0.1 km and (ii) Rs. 100
- 24. Suppose the car market is perfectly competitive and each firm has the same cost structure. There are 1000 firms in the industry. The market demand and cost schedules are given below.

Market Demand

Market Dem: Price (lacs/	and 3.65	5.20	6.80	8.40	10.00	11.60	13.20
per car)					200	250	200
Quantity	500	450	400	350	300	250	200
(thousands per year)							<u> </u>

Coete per firm (Rs. lacs)

Costs per	firm (Ks.			1050	400	450	500
Output	200	250	300	350			
	-	7.00	7.65	8.40	10.00	12.40	12.70
MC	6.40				7.50	. 8.00	9.00
AVC	7.80	7.00	7.10	7.20			11.00
ATC	12.80	11.00	1043	10.06	10.00	10.22	11.00

In the long run

- (a) Some firms will exit the industry, but others will remain
- (b) Some firms will enter the industry
- (c) The number of firms will remain the same
- (d) The industry will close down
- 25. Abhik's and Brinda's demand curves for apples are given by

$$p = 20 - q (Abhik)$$

$$p = 5 - (q/2)$$
 (Brinda)

where p,
$$q \ge 0$$
 for each.

Suppose these are the only two consumers in the market, and that the market supply function is given by: p = 2 + Q. Then the equilibrium quantity in the market is:

- (a) 12 apples
- (b) 9 apples
- (c) 6 apples
- (d) 3 apples
- 26. A farmer's demand for wheat is given by the function:

$$q = 25 + m/20p$$

where m is his money income and p is the price of wheat. Let the farmer's money income be Rs. 1000. Suppose that initially, the farmer purchases wheat in the market for Rs. 10 per kg. Now, consider a situation where the farmer obtains a BPL ćard which allows him to purchase up to 35 kg of wheat for Rs. 5 per kg. What will be the increase in his demand for wheat attributable to the Slutsky substitution effect?

- (a) 3.5 kg
- (b) 4.0 kg
- (c) 4.5 kg
- (d) 5.0 kg

Answer the next four questions using the following information. An economy has two agents (1 and 2) and 3 units each of two goods, X and Y. An allocation in this economy is defined as a tuple $((x_0, y_0), (x_1, y_1), (x_2, y_2))$ of non-negative real numbers, where (x_1, y_1) and (x_2, y_2) are the amounts of goods X and Y consumed by Agents 1 and 2 respectively, and (x_0, y_0) are the amounts of the two goods left over after the consumption of the two agents (i.e., $x_0 = 3 - x_1 - x_2$, $y_0 = 3 - y_1 - y_2$). The agents' ability to consume is limited, so that for each Agent i=1,2, (x_i, y_i) must satisfy

 $x_i^2 + y_i^2 \le 12$. Agent 1 is higher on the social ladder and gets to choose his consumption bundle (x_1, y_1) first. Agent 2 chooses her consumption bundle from what remains of the two goods after Agent 1 has chosen. An equilibrium for this economy is an allocation such that

(1). (x_1, y_1) maximizes Agent 1's utility subject to the constraints

$$x_1 \le 3$$
, $y_1 \le 3$, $x_1^2 + y_2^2 \le 12$, and

(2). (x_2, y_2) maximizes Agent 2's utility subject to the constraints

$$x_2 \le 3 - x_1, y_2 \le 3 - y_1, x_2^2 + y_2^2 \le 12.$$

It is given that Agent 1's utility function $u_1(x_1, y_1) = x_1^2 y_1$ and Agent 2's utility function $u_2(x_2, y_2) = ax_2 + y_2$, where 'a' is a given positive number.

- 27. Which one of the allocations $((x_0, y_0), (x_1, y_1), (x_2, y_2))$ specified below is an equilibrium for this economy?
 - (a) $((0,0),(3,\sqrt{3}),(0,3-\sqrt{3}))$
 - (b) $((0,0),(\sqrt{6},\sqrt{6}),(3-\sqrt{6},3-\sqrt{6}))$
 - (c) $((0,0),(2.5,\sqrt{5.75}),(0.5,3-\sqrt{5.75}))$
 - (d) $((0,0),(\sqrt{8},2),(3-\sqrt{8},1))$
- 28. Let a=1, for Agent 2's utility function. Then, the equilibrium allocation in the above question is

(a) Pareto efficient, because the slopes of the Agents' indifference curves are

tangent at that allocation.

(b) Not Pareto efficient, because the slopes of the Agents' indifference curves are not tangent at that allocation.

(c) Pareto efficient, because there is a bound on Agent 1's ability to consume.

- (d) Not Pareto efficient, as Agent 2 can be made better off without making Agent 1 worse off.
- 29. Suppose there was no bound on the ability of any agent to consume, and you could choose the value of the parameter 'a' in Agent 2's utility function. For what value of 'a' would the equilibrium in Question 1 be efficient?
 - (a) 1
 - (b) $\sqrt{2}$
 - (c) $\sqrt{8}$
 - (d) 2
- 30. Now suppose that Agent 2 is higher on the social ladder than Agent 1, so Agent 2 gets to choose her consumption bundle before Agent 1 does. All other features of the economy are unchanged. If a = 2, which one of the allocations $((x_0, y_0), (x_1, y_1), (x_2, y_2))$ below is an equilibrium for this modified economy?
 - (a) $((0,0),(3,\sqrt{3}),(0,3-\sqrt{3}))$
 - (b) $((0,0),(3-\sqrt{48/5},3-\sqrt{12/5}),(\sqrt{48/5},\sqrt{12/5}))$
 - (c) $((0,0),(0,3-\sqrt{3}),(3,\sqrt{3}))$
 - (d) $((0,0),(2,3-\sqrt{8}),(1,\sqrt{8}))$

The following information applies to the next four questions. Consider an economy where the nominal wage rate (W) is set by the workers and it depends on the expected price level (P') and the rate of unemployment (u) in the following way: $W = P' \cdot (1 - \alpha u)$, where α is a parameter; $0 < \alpha < 1$. The actual price level (P) on the other hand is set by the producers who charge a mark up over the nominal wage rate so that: $P = (1 + \lambda)W$, where $\lambda > 0$ is another parameter.

- 31. If the workers are always able to correctly guess the price level then the rate of unemployment will always be maintained at a level which is given by:
 - (a) $\frac{1}{1+\lambda}$;
 - (b) $\frac{\alpha}{1+\lambda}$;
 - (c) $\frac{1}{(1+\lambda)\alpha}$
 - (d) $\frac{1+\alpha}{1+\lambda}$
- 32. There will be always be full employment of the aggregate stock of labour force if and only if the expected and the actual price level are related in the following way:

(a)
$$\frac{P}{P^e} = 1$$

(b)
$$\frac{P}{P^e} = 1 + \lambda$$

(c)
$$\frac{P}{P^c} = \frac{1+\lambda}{1-\alpha}$$

(d)
$$\frac{P}{P^e} = (1 + \lambda)(1 - \alpha)$$

The following additional information applies to the next two questions. In addition to the information given for the above two questions, suppose the production technology is such that one employed worker can produce one unit of output. Let Y, N, and \overline{L} denote the level of output, the level of employment and the aggregate stock of labour force respectively. On the basis of the wage and price information given in the previous questions, work out a relationship between P, P^{ϵ} and Y and answer the following two questions:

- 33. An increase in output ceteris paribus leads to
 - (a) an increase in the actual price level
 - (b) a decrease in the actual price level
 - (c) the actual price level will remain unchanged
 - (d) given information is not sufficient to conclude anything about the change in actual price level
- 34. An increase in the aggregate stock of labor force ceteris paribus leads to
 - (a) an increase in the actual price level
 - (b) a decrease in the actual price level
 - (c) the actual price level will remain unchanged
 - (d) given information is not sufficient to conclude anything about the change in actual price level

The following information applies to the next two questions. Consider the following macroeconomic model. The goods market is characterized by the following set of equations:

$$C = \alpha_0 + \alpha_1 Y$$

$$I = \beta_0 + \beta_1 Y - \beta_2 i$$

$$G = \overline{G}$$
 (exogenously given)

where $\alpha_0, \alpha_1, \alpha_2, \beta_0, \beta_1, \beta_2$ are all positive constants and $\alpha_1 + \beta_1 < 1$.

The money market equilibrium condition is given by:

$$\frac{\overline{M}}{P} = \gamma_1 Y - \gamma_2 i$$
; γ_1, γ_2 positive constants.

Answer the following two questions on the basis of this model:

35. If interest rate(i) increases by one unit, to maintain equilibrium in the goods market, income level (Y) has to decrease by

(a)
$$\frac{\beta_2}{1-(\alpha_1+\beta_1)}$$
 units

(b)
$$\frac{1}{1-(\alpha_1+\beta_1)}$$
 units

(c)
$$\frac{1}{1 - (\alpha_1 + \beta_1) + \frac{\gamma_1}{\gamma_2} \beta_2}$$
 units

(d)
$$\frac{1}{1-(\alpha_1+\beta_1)+\frac{\gamma_1}{\gamma_2}\alpha_2}$$
 units

36. A unit increase in government expenditure (G) will increase the equilibrium income level (Y) by

(a)
$$\frac{\beta_2}{1-(\alpha_1+\beta_1)}$$
 units

(b)
$$\frac{1}{1-(\alpha_1+\beta_1)}$$
 units

(c)
$$\frac{1}{1-(\alpha_1+\beta_1)+\frac{\gamma_1}{\gamma_2}\beta_2}$$
 units

(d)
$$\frac{1}{1 - (\alpha_1 + \beta_1) + \frac{\gamma_1}{\gamma_2} \alpha_2}$$
 units

The following information applies to the next two questions. Savitri has got a job in a household for 2 months with wages w_1 and w_2 respectively. She plans for her consumption in the two months (denoted by, c_1 and c_2 respectively) so as to maximize

her utility given by $\log c_1 + \frac{1}{1+\delta} \log c_2$, where $\delta > 0$ is the discount rate. She is also allowed to borrow from her employer in the first month which she has to repay, with interest at the rate r, from her second month's earnings. Alternatively she can save some

of her wages in the first month and keep it in the bank to earn an interest at the same rate r. In this framework answer the following two questions:

37. Savitri will optimally decide to borrow from her employer in the first month if and only if the following condition is satisfied:

(a)
$$w_2 > (1+r)w_1$$

(b)
$$(1+\delta) > (1+r)$$

(c)
$$(1+\delta)w_2 > (1+r)w_1$$

(d)
$$(1+\delta) < (1+r)$$

- 38. Assuming that the above condition is satisfied, when the discount rate (δ) goes up, her borrowing
 - (a) goes up
 - (b) goes down
 - (c) does not change
 - (d) cannot say on the basis of the given information
- 39. Consider two open economies with fixed exchange rates, when the exchange rate is unity. The economies are characterized by the following set of equations, where i = 1,2:

$$C_i = c_{01} + c_{1i} (Y_i - T_i)$$

$$I_i = \overline{I}_i$$

$$G_i = \overline{G}_i$$

$$T_i = t_i Y_i$$

$$M_i = m_{0i} + m_{1i}Y_i$$

If
$$c_{01} = c_{02} = 200$$
; $c_{11} = c_{12} = 0.5$; $I_1 = I_2 = 250$; $G_1 = 114$; $G_2 = 120$; $t_1 = t_2 = 0.4$;

 $m_{01} = m_{02} = 40$; $m_{11} = 0.05$; $m_{12} = 0.3$ then which of the following is true?

- (a) Country 1 has a higher equilibrium level of output than Country 2 and it runs a trade deficit vis-à-vis Country 2
- (b) Country 1 has a lower equilibrium level of output than Country 2 and it runs a trade deficit vis-à-vis Country 2
- (c) Country 1 has a higher equilibrium level of output than Country 2 and it runs a trade surplus vis-à-vis Country 2
- (d) Country 1 has a lower equilibrium level of output than Country 2 and it runs a trade surplus vis-à-vis Country 2
- 40. In the Mundell-Fleming model of a small open economy with flexible exchange rates and perfect capital mobility, suppose the economy is initially in equilibrium. If lump sum taxes are increased, what happens to the *equilibrium* levels of the country's (i) GDP; (ii) interest rate and (iii) exchange rate?
 - (a) (i) falls, (ii) falls, (iii) appreciates
 - (b) (i) and (ii) remain unchanged; (iii) depreciates
 - (c) (i) falls, (ii) and (iii) remain unchanged.
 - (d) All three remain unchanged.
- 41. $f: \mathbb{R}^n \to \mathbb{R}$ is convex if and only if
 - (a) $\{(x, r) \Re^n \times \Re \mid f(x) \le r\}$ is convex
 - (b) $\{(x, r) \Re^n \times \Re \mid f(x) \ge r\}$ is convex
 - (c) $\{x \in \mathfrak{R}^n \mid f(x) \le r\}$ is convex for every $r \in \mathfrak{R}$
 - (d) $\{x \in \mathfrak{R}^n \mid f(x) \ge r\}$ is convex for every $r \in \mathfrak{R}$

```
42. If f: \mathfrak{R}_+ \to \mathfrak{R} is defined by f(x) = \int_x^{x^2} e^t dt, then the derivative of f at x > 0 is
```

- (a) $2xe^{x^2} e^x$
- (b) $2xe^{x^2} + e^x$
- (c) $(2x-1) e^{x^2}$
- (d) $(2x-1) e^x$

43. The sequence
$$(x_n)$$
, where $x_n = (-1)^n (1 + n^{-1})$ and $n = 1, 2, ...$

- (a) converges to 1
- (b) converges to −1
- (c) converges to 1 and -1
- (d) converges to neither 1 nor -1

44. The set
$$\bigcap_{n=1}^{\infty} (-1 - n^{-1}, 1 + n^{-1})$$
 is identical to

- (a)(-1,1]
- (b) [-1, 1)
- (c)(-1,1)
- (d)[-1,1]

45. The set
$$\bigcup_{n=1}^{\infty} [-1 + n^{-1}, 1 - n^{-1}]$$
 is identical to

- (a)(-1,1]
- (b) [-1, 1)
- (c)(-1,1)
- (d)[-1,1]

46. For
$$x, y \in \mathbb{R}^n$$
, let $d(x, y) = \max\{|x_i - y_i| \mid i = 1, ..., n\}$. Which of the following relations holds for all $x, y, z \in \mathbb{R}^n$?

- (a) d(x, z) = d(x, y) + d(y, z)
- (b) d(x, z) > d(x, y) + d(y, z)
- (c) $d(x, z) \ge d(x, y) + d(y, z)$
- (d) $d(x, z) \le d(x, y) + d(y, z)$

47. Given sets X, Y, let
$$X \times Y = \{(x, y) \mid x \in X \text{ and } y \in Y \}$$
, and let $X - Y = \{x \in X \mid x \notin Y \}$. Which of the following formulae is generally correct for sets A, B and C?

- (a) $(A B) \times C = (B \times C) (A \times C)$
- (b) $(A B) \times C = (A \times C) (B \times C)$
- (c) $(A B) \times C = (A \times C) B$
- (d) $(A B) \times C = A (B \times C)$

48. Suppose $f: \mathbb{R}^2 \to \mathbb{R}$ is defined by z = xy. At (0, 0) this function

(a) Attains a maximum

- (b) Attains a minimum
- (c) Attains a saddle point
- (d) Is undefined
- 49. What is the maximum value of the function in the previous question, subject to the constraints x > 0, y > 0, and 2x+y = 6?
 - (a) 2.5
 - (b) 4
 - (c) 4.5
 - (d)9
- 50. "Beautiful cities repel people. Look at India's most beautiful cities they are among the least populated cities of the country". Which of the following statements illustrates a method of reasoning most similar to the one in the argument above?
 - (a) Children who are spanked tend to be more naughty than other children. Hence if a child is not spanked, that child is less likely to be naughty.
 - (b) Pesticides are known to cause asthma among some people. However, most asthmatic people tend to live in regions where pesticides are not commonly used.
 - (c) This software program helps increase the work efficiency of its users. As a result, these users have more free time for other activities.
 - (d) During warm weather, my crops suffer from pests more than during cooler weather. Therefore, a warm environment must help pests to multiply.
- 51. The average travel time to a distant city is whours by train or z hours by bus. A man cannot decide whether to take the train or the bus, so he tosses a coin. What is his expected travel time?
 - (a) 2(w+z)
 - (b) 2(w+z)/w-z
 - (c) (w+z+2)/2
 - (d) None of the above
- 52. A class has 6 students, randomly divided into two teams, A and B, for a race. What is the probability that the three runners in team A will come in first, second and third?
 - (a) 3!/6!
 - (b) 1/6!
 - (c) (3!)2/6!
 - (d) 3/6!
- 53. Suppose that each person out of a group of 4 friends is randomly assigned to one of 6 classes. What is the probability that no class has more than one person from this group?
 - (a) 6!/4!
 - (b) 5/18
 - (c) 4/6
 - (d) 6/4!

- 54. A continuous random variable has the probability density function f(x) = 1/3, for x between -1 and +2, and 0 elsewhere. Its mean, variance and median are:
 - (a) $(1, \frac{3}{4}, \frac{1}{2})$
 - (b) (1/2, 3/4, 1/2)
 - (c) $(\frac{1}{2}, 1, 1)$
 - (d) (½, 1, ½)
- 55. The joint probability distribution of A and W for a given population is as follows, where A is the individual's age in years and W is the weight she can lift.

W	10 kilos 20 kilos 30 kilos	A 15 years 0.03 0.02 0.01	25 years 0.16 0.13 0.09	40 years 0.14 0.11 0.08	60 years 0.12 0.09 0.01	80 years 0.01 0.00 0.00
---	----------------------------------	---------------------------------------	----------------------------------	----------------------------------	----------------------------------	----------------------------------

The expectation of the marginal distribution of A is:

- (a) 36.7 years
- (b) 37.6 years
- (c) 35.6 years
- (d) 38.6 years
- 56. In a survey of 400 likely voters, 215 responded that they would vote for the ruling party and 185 responded that they would vote for the opposition party. Let p denote the fraction of all likely voters who preferred the ruling party at the time of the survey, and let \hat{p} be the fraction of survey respondents who preferred the ruling party. The standard error of \hat{p} is:
 - (a) 0.025
 - (b) 0.035
 - (c) 0.045
 - (d) 0.055
- 57. Let X and Y be two random variables with E[X] = 3, E[Y] = 0, V[X] = 4, V[Y] = 25, and E[XY] = 5. Find (i) Cov[X, Y]; (ii) the Pearsonian coefficient of correlation between X and Y ($\rho_{X,Y}$); (iii) V[X+Y].
 - (a) 0.5, 5, 39
 - (b) 5, 0.5, 34
 - (c) 5, 5, 39
 - (d) 5, 0.5, 39
- 58. If Y is a binomial random variable with parameters n = 4 and p = 0.78, calculate Prob(Y \geq 3) to 2 decimal places.
 - (a) 0.15
 - (b) 0.21
 - (c) 0.64
 - (d) 0.79

For the following two questions please note that the two-tailed 5% critical value for a stand ordized normal distribution is ± 1.96 and the corresponding value for a one-tailed test is ± 1.645 . At the 1% level of significance, the critical value for a two-tailed test is ± 2.58 and the corresponding value for a one-tailed test is ± 2.33 .

59. An examination was given to two classes consisting of 40 and 50 students respectively. In the first class the mean grade was 74 with a standard deviation of 8, while in the second class the mean grade was 78 with a standard deviation of 7. On the basis of a two-tailed test, is there a significant difference between the performance of the two classes at a level of significance of 5% and 1%?

There is no significant difference in the performance of the two classes at the 5% and 1% levels of significance

- (b) There is a significant difference in the performance of the classes at the 5% level but no significant difference at the 1% level of significance
- (c) There is a significant difference in the performance of the classes at the 1% level but no significant difference at the 5% level of significance
- (d) There is a significant difference in performance at both the 5% and 1% levels
- 60. A sample poll of 300 voters from District A and 200 voters from District B showed that 56% and 48% respectively were in favour of a given candidate. At a level of significance of 5%, test the hypothesis that (a) there is a difference between the districts, (b) the candidate is preferred in District A.

(a) There is no significant difference between the districts and the candidate is not preferred in District A

(b) There is no significant difference between the districts and the candidate is preferred in District A

(c) There is a significant difference between the districts and the candidate is not preferred in District A

(d) There is a significant difference between the districts and the candidate is preferred in District A

After you finish, hand in this booklet along with your bubble sheet to the invigilators before leaving the examination hall.